

# Privacy–friendly Aggregation for the Smart-grid

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# Introduction

All Around  
The World

- Why Aggregation?
  - Privacy Concern (personal data leakage)
  - Security Concern (fraud)
  - Safety Concern (leakage of gas)
  - Forecasting
  - ...
- The meter here can also from the system of water or gas ...

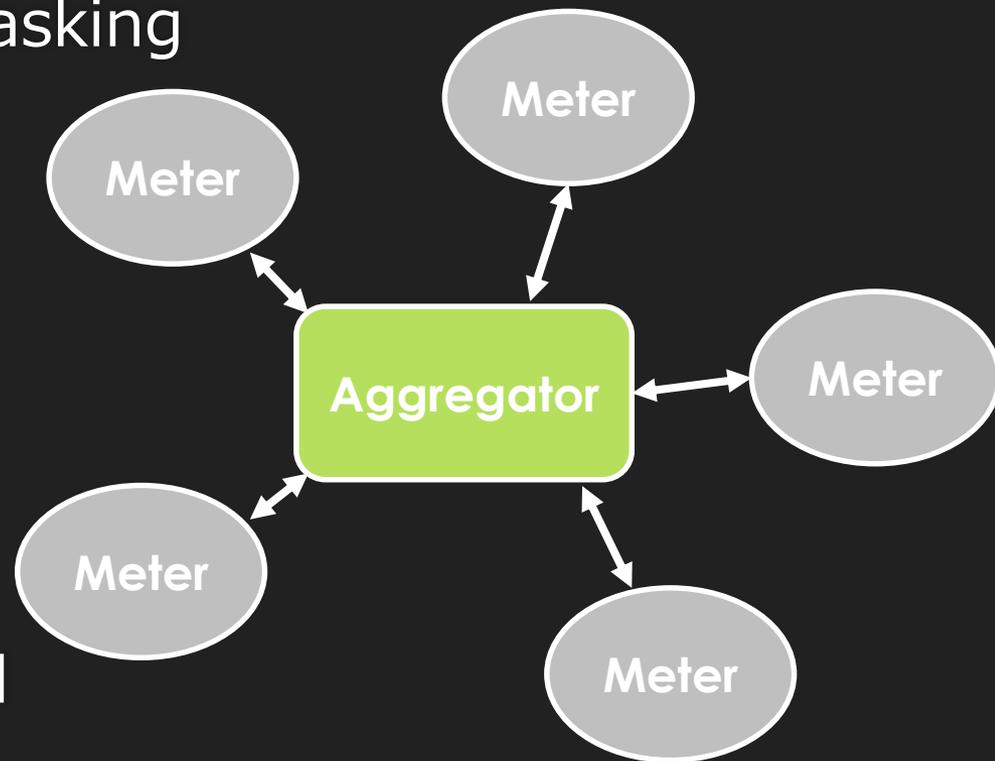
# Introduction

- Consumption( $c_{i,j}$ ) Masking

- $i$ : round,  $j$ : meter

- Masking values should cancel out after aggregation

- Should be encrypted



# Basic Protocol Types

- Aggregation Protocol

- Blinded value:  $x_{i,j} + c_{i,j}$
- Result =  $\sum(c_{i,j})$  ;  $\sum(x_{i,j}) = 0$

- Comparison Protocol

- Blinded value:  $g_i^{x_j + c_{i,j}}$
- Result =  $g_i^{\sum c_{i,j}}$  ,  $g_i \in$  Diffie–Hellman group  $\mathbb{G}$
- Compare the result and its guess  $g_i^{c_a}$

- Masking value:  $x_{i,j}$

# Concrete Protocols

## ○ Interactive Protocol

- Each user  $j$  have private key ( $X_j$ ) and public key ( $Pub_j$ )
- Choose  $p$  leaders from  $n$  users:  $l_1, \dots, l_p$
- Everyone generates  $p$  shares:  $s_{i,1}, \dots, s_{i,p}$
- After receiving the shares(encrypted), leaders can compute their own share such that the sum of these shares is zero and replace the original one
- The main share  $s_j$  for user  $j$  is the sum of all his shares
- Aggregation or Comparison Protocol

# Concrete Protocols

- Diffie-Hellman Key-Exchange Based Protocol
  - Each meter  $j$  has its own secret key  $X_j$
  - In each round  $i$ , it will have a generator of  $\mathbb{G}$   $g_i = H(i)$ , and also each meter  $j$  has its public key  $Pub_{i,j} = g_i^{X_j}$
  - $g_i^{x_j} = \prod_{k \neq j} Pub_{i,k}^{(-1)^{k < j} \cdot X_j}$
  - $\sum_j x_j = 0$
  - Only Comparison Protocol

# Concrete Protocols

- Diffie-Hellman and Bilinear-map Based Protocol
  - Similar to the previous one but only need one public key ( $Pub_j$ ) for each mdeater:  $Pub_j = \hat{g}_0^{X_j}$
  - Bi-linear function  $e(\mathbb{G}_1, \mathbb{G}_2) \rightarrow \mathbb{G}_T$
  - $g_i^{x_j} = (\prod_{k \neq j} e(Pub_k, \hat{g}_i)^{(-1)^{k < j}})^{X_j}$
  - $\hat{g}_0$ : generator of  $\mathbb{G}_1$  ;  $\hat{g}_i = H(i)$ ,  $H(\{0,1\}^*) \rightarrow \mathbb{G}_2$
  - Also only Comparison Protocol

# Concrete Protocols

- Low-overhead Protocol

- Each pair of meter has their shared key  $K_{j,k} = H(Pub_k^{X_j})$

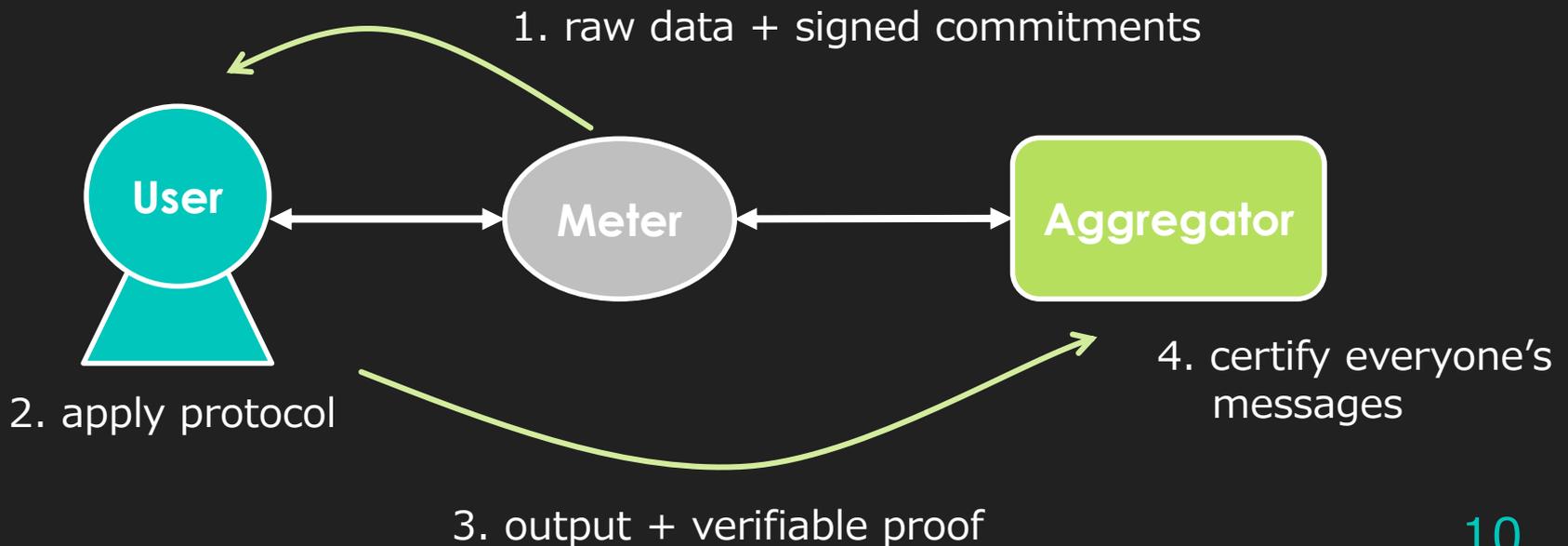
- ,where  $Pub_k = g^{X_k}$ ,  $H(\{0,1\}^*) \rightarrow \mathbb{G}$ ,  $g$ : generator of  $\mathbb{G}$

- $x_{i,j} = \sum_{k \neq j} (-1)^{k < j} H(K_{j,k} || i)$

- Aggregation or Comparison Protocol

# Comparison

- Cryptographic Verifiability
  - Transmit data with commitments and certifications



# Comparison

## ○ Computation & Communication Overheads

	Initialization	Communication	Computation
Interactive (agg)	$O(N^2) \cdot PK$	$O(N \cdot p) \cdot \mathbb{Z}_q$	$O(p) \cdot \text{Enc}$
Interactive (comp)	$O(N^2) \cdot PK$	$O(N) \cdot \mathbb{G}$	$O(1) \cdot E$
DH	$+O(N \cdot p) \cdot \mathbb{Z}_q$ $O(N^2) \cdot \mathbb{G}$	$O(N^2) \cdot \mathbb{G}$	$O(N) \cdot M + O(1) \cdot E$
Pairing	$O(N^2) \cdot \mathbb{G}$	$O(N) \cdot \mathbb{G}$	$O(N) \cdot P + O(1) \cdot E$
Low-overhead (agg)	$O(N^2) \cdot \mathbb{G}$	$O(N) \cdot \mathbb{Z}_{2^{32}}$	$O(N) \cdot H$
GC [4]	$O(N^2) \cdot PK$	$O(N^2) \cdot \mathbb{Z}_{n^2}$	$O(N) \cdot \text{Enc} + O(1) \cdot \text{Dec}$

**Table 1.** Performance comparison:  $PK$ .. size of public keys,  $|\mathbb{Z}_x|$ ,  $\mathbb{G}$ .. size of algebraic group,  $\text{Enc}$ ,  $\text{Dec}$ ,  $E$ ,  $M$ ,  $H$ .. cost of encryption, decryption, exponentiation, multiplication, or hash function evaluation respectively.

# Comparison

- Availability
  - Critical parts → inside meter
- Privacy
  - Passive attackers
  - Active attackers
- Forward Secrecy
  - Interactive and DH based protocol

# Conclusion

**Questions?**

**anyone**

**Thank you!**